



Electrokinetic response of “standard particles” and more...

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System

1) "standard" particles :

⇒ constant charge = $0,04 \text{ C/m}^2$ (sulfate latex)

⇒ radius = 265 nm (TEM)

⇒ monodisperse

⇒ Suspending medium: demi-water + salts

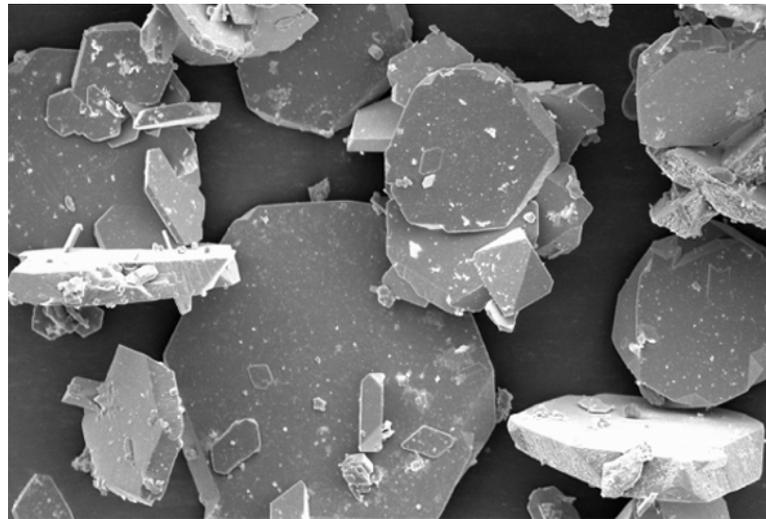


System

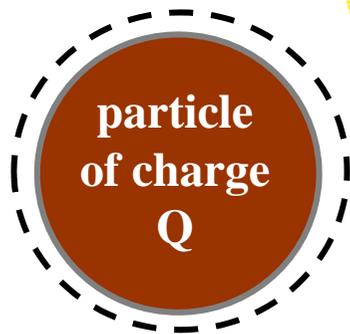
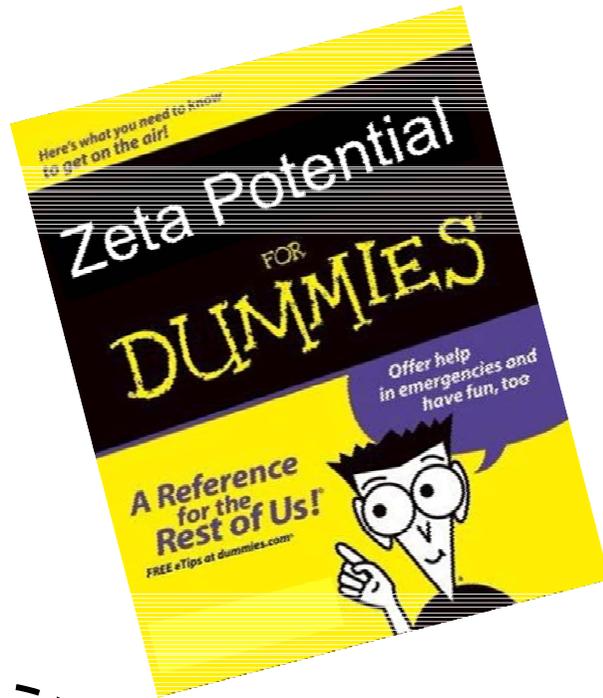
2) "more" = non-spherical particles :

⇒ kaolinite, gibbsite, goethite (clays, oxides)

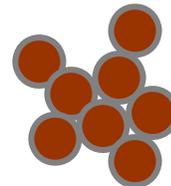
⇒ non-ideal



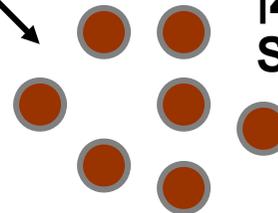
Zeta Potential



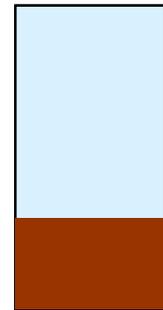
slip plane where the zeta potential ζ is defined $\zeta=f(Q)$



$|ZP| = |\zeta| < 25 \text{ mV}$
AGGREGATE



$|ZP| = |\zeta| \gg 25 \text{ mV}$
STABLE



Application

zeta pot. > interactions > rheology



Influence of anions on the rheological properties of clay mineral dispersions

Author(s): Penner, D (Penner, D); Lagaly, G (Lagaly, G)

Source: APPLIED CLAY SCIENCE Volume: 19 Issue: 1-6 Special Issue: SI Pages: 131-142 DOI: 10.1016/S0169-1317(01)00052-7 Published: JUL 2001

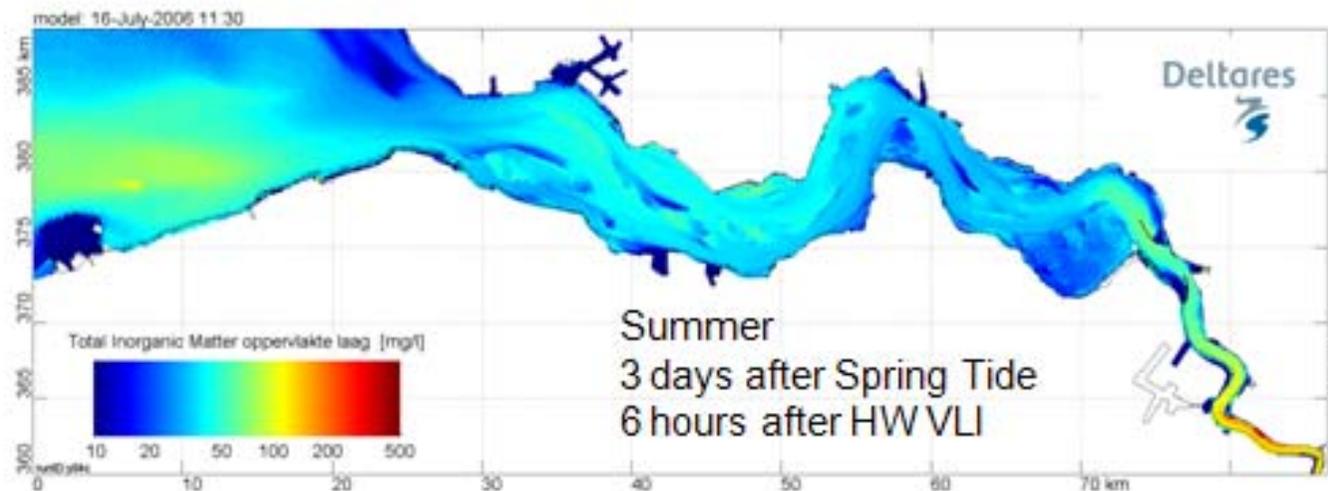
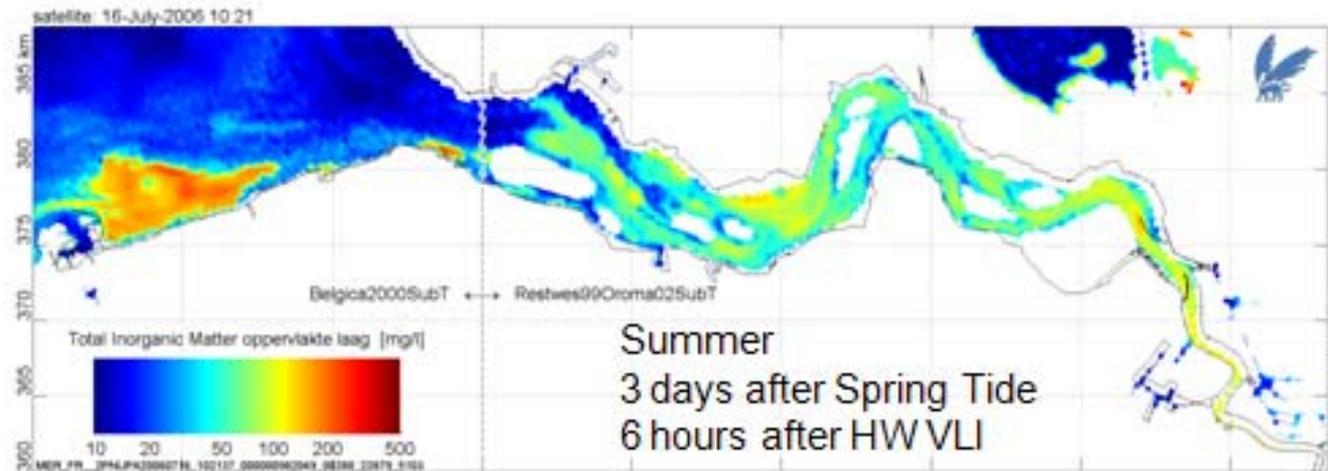
Times Cited: 41 (from Web of Science)

Cited References: 72 [[view related records](#)]  [Citation Map](#)

Conference: European Clay Conference on Surface Modification of Clay Minerals (EUROCLAY '99) Location: KRAKOW, POLAND Date: SEP 05-09, 1999

Abstract: The flow behavior of sodium montmorillonite dispersions and kaolin slurries can have different responses to anionic dispersants. Viscosity, pH, and dynamic mobility measurements using a variety of salts help elucidate this important observation. The flow behavior is determined not only by the counterions but also by the colons (anions) surrounding the clay mineral particles. The viscosity of sodium montmorillonite dispersions with increasing salt or acid concentration decreased to a minimum, then increased sharply. The concentration at this point was identified as the critical coagulation concentration, $c(K)$. Salts with multivalent anions such as sulphates and phosphates increased the critical coagulation concentration. $\text{Na}_4\text{P}_2\text{O}_7$ actually impeded coagulation. The liquefying effect of these anions was counterbalanced by the protons of acidic salts such as NaHSO_4 , Na_2HPO_4 , and NaH_2PO_4 and by acids. The critical coagulation concentration for sodium montmorillonite was a function of the montmorillonite concentration and the type of ion. In 2% sodium montmorillonite dispersions, $c(K)$ for sodium chloride and sulphate was higher than $c(K)$ in dilute dispersions (0.025%). For the strongly liquefying agents Na_2HPO_4 , NaH_2PO_4 , and H_3PO_4 , the opposite was true. The $c(K)$ values for the dilute dispersion were 1100, 460, and 32 mmol/l respectively, and for the 2% dispersion 80, 40, and 10 mmol/l. Kaolinite dispersions in contrast to sodium montmorillonite showed the pronounced liquefying effect of multivalent anions up to high salt concentrations. The data underscored the complexity of dispersed systems. For example, the dynamic mobility of the particles and the viscosity of the system were not always directly related. An interesting aspect concerns the dynamic mobility of the montmorillonite and kaolinite particles which in different ways changed with concentration of salts and acids. (C) 2001 Elsevier Science B.V. All rights reserved.

Application



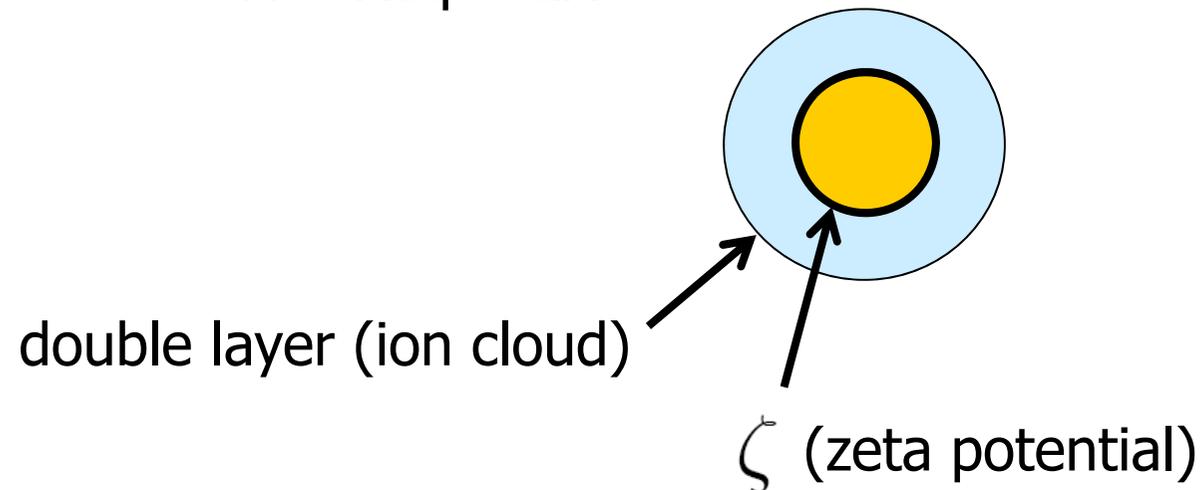
Assumptions

$T = \text{constant}$ (no "thermo-dynamic")

$E = \text{applied electric field}$ (but "electro-dynamic")

$E \text{ (V/cm)} \ll \text{zeta potential (mV)} / \text{double layer (nm)}$

$$\Rightarrow X = X_{eq} + dX$$



Shear plane = surface particle : $\zeta = \Psi_0$

Relation charge / potential at eq.

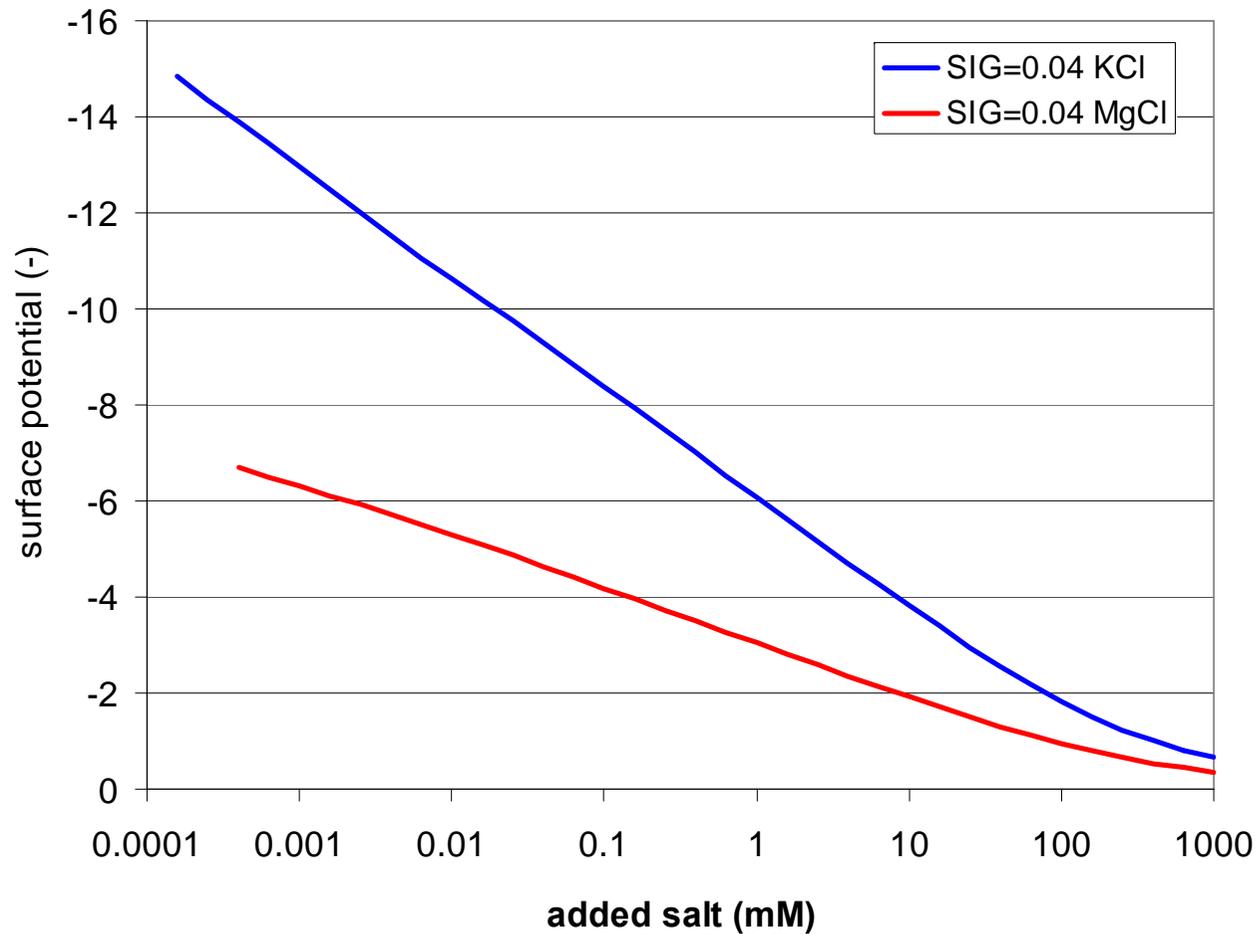
$$\left(\frac{d\Psi_{eq}}{dx} \right)_{x=0} = \frac{-\sigma}{\varepsilon}$$

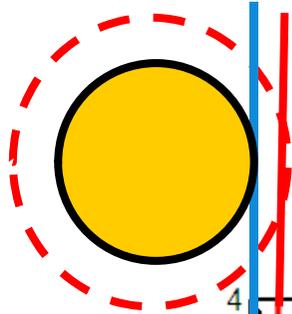
We will assume a **constant surface charge** :

fixe charge => find the zeta potential for each ionic strength using (PB) + bisection method

$$\nabla^2 \Psi_{eq} = \kappa^2 \sinh(\Psi_{eq}) \quad \kappa^{-1} = \sqrt{\frac{\varepsilon_0 \varepsilon_1 kT}{2e^2 N_A C_s}}$$

Surface potential / added salt in case of a constant charge

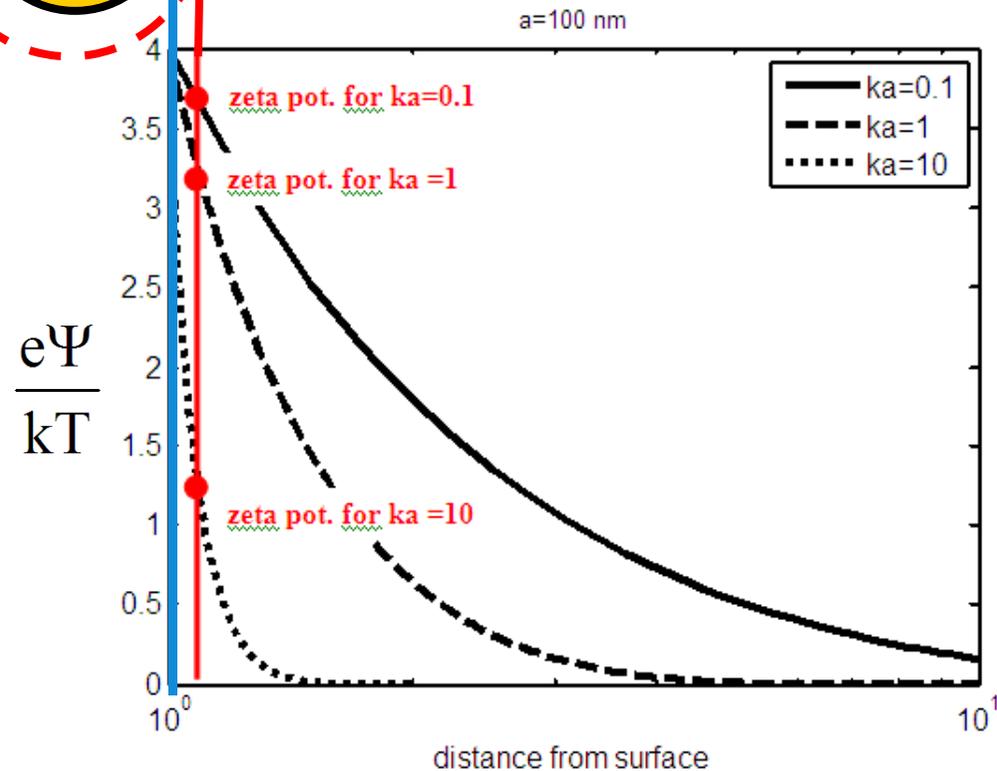




constant surface potential Ψ_0

The shear plane is at d (nm) from the surface

The zeta potential ζ = potential at shear plane



Constant surface potential but zeta potential decreases with ionic strength when $d \neq 0$

Standard electrokinetic equations

Poisson :
$$\nabla^2 \delta\Psi = \frac{-1}{\varepsilon_0 \varepsilon_1} \sum e z_i \delta n_i$$

Conservation of mass:

$$\mathbf{J}_i = n_{i,\text{eq}} \mathbf{u} - n_{i,\text{eq}} D \nabla \left[\frac{z_i e}{kT} \delta\Psi + \frac{\delta n_i}{n_{i,\text{eq}}} \right]$$

$$\frac{\partial \delta n_i}{\partial t} + \nabla \cdot \mathbf{J}_i = 0.$$

Note:

$$\mathbf{u}_{\text{tot}} = \mathbf{u}_{\text{eq}} + \delta \mathbf{u} = \delta \mathbf{u} \equiv \mathbf{u}.$$

Standard electrokinetic equations

Boundary conditions

Potential :
$$\varepsilon_0 \varepsilon_2 \left(\frac{\partial(\delta\Psi_2)}{\partial r} \right)_{r=a} = \varepsilon_0 \varepsilon_1 \left(\frac{\partial(\delta\Psi)}{\partial r} \right)_{r=a}$$

$$\delta\Psi_2(a) = \delta\Psi(a), \quad (\Delta\delta\Psi_2 = 0)$$

No flux:
$$(\mathbf{J}_i \cdot \mathbf{e}_r)_{r=a} = 0$$

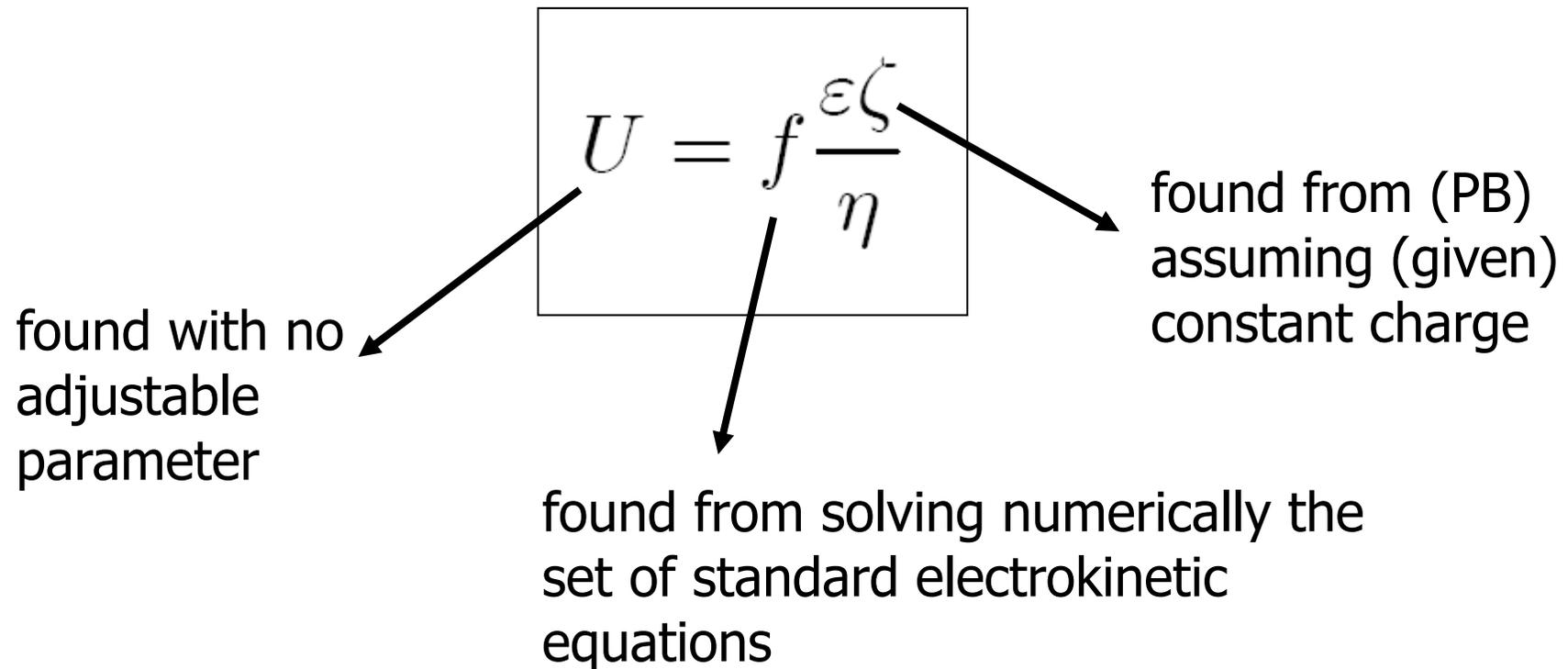
No slip:
$$\mathbf{u}(r = a) = \mathbf{0}$$

$$\mathbf{u}(\infty) = -\mathbf{U}$$

Electrophoresis

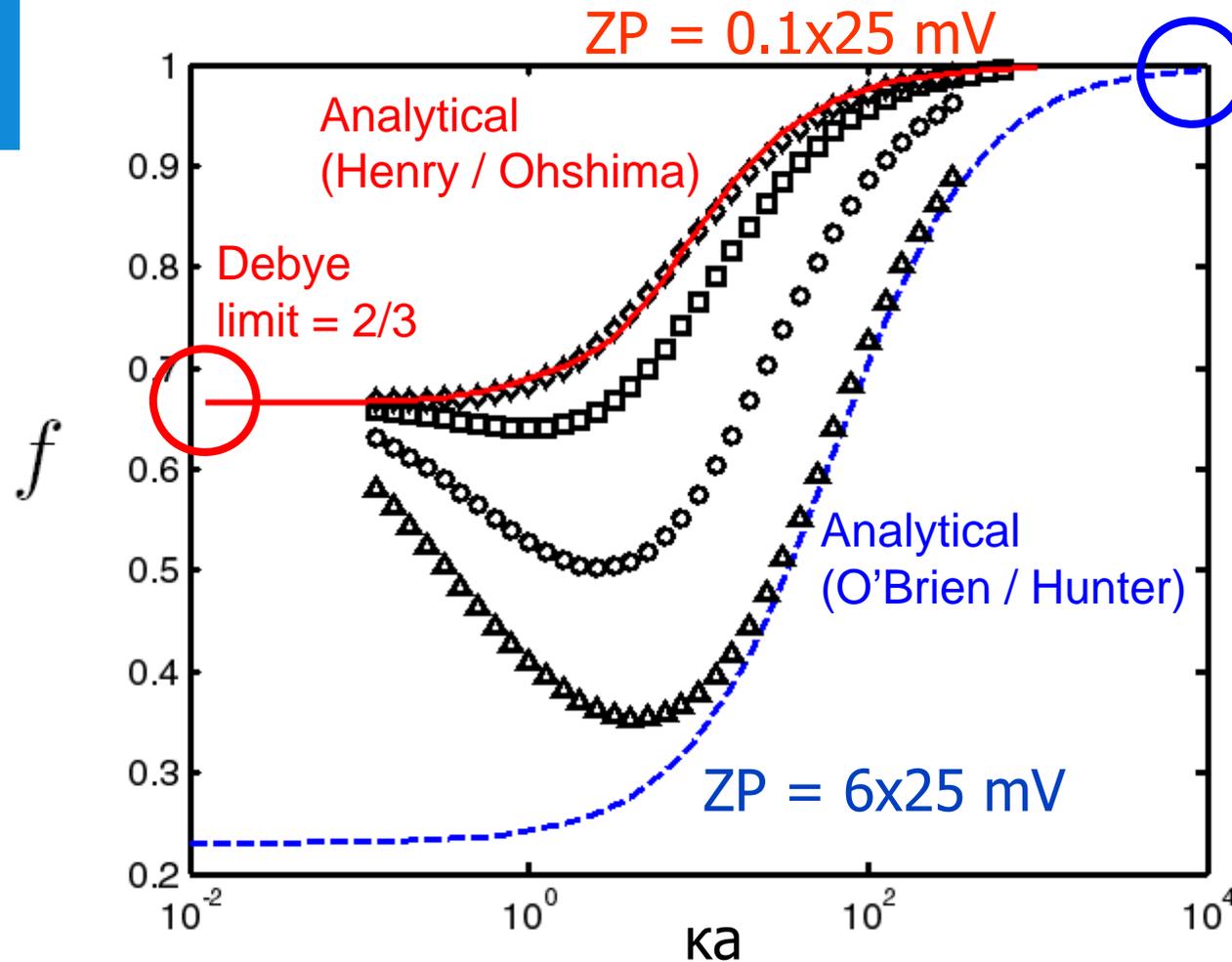
standard electrokinetic equations

relation electrophoretic mobility / zeta potential:



Electrophoresis

constant zeta potential



Smoluchowsky limit = 1

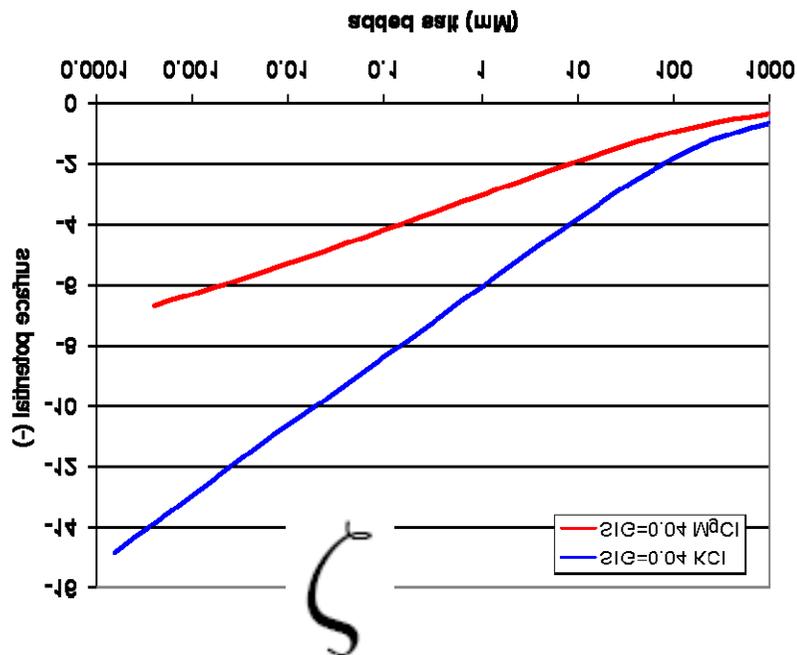
$$U = f \frac{\epsilon \zeta}{\eta}$$

symbols: num. simulations

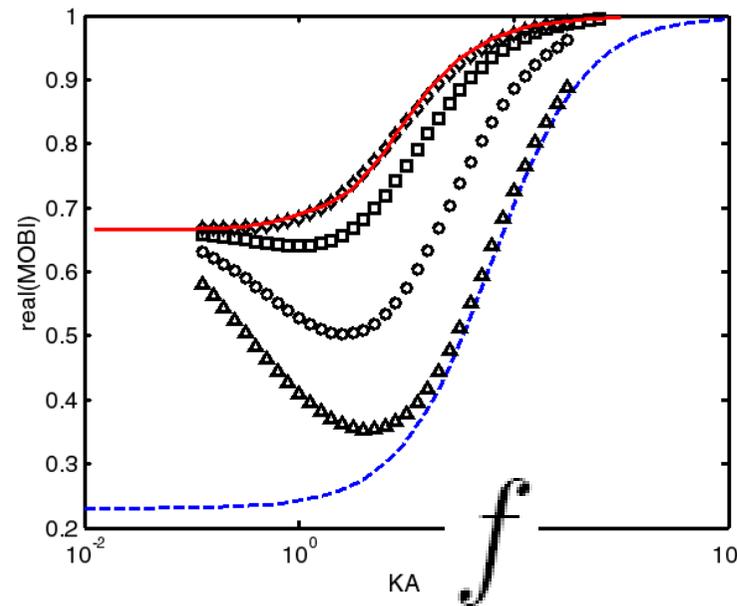
Electrophoresis / added salt constant charge

$$f \zeta =$$

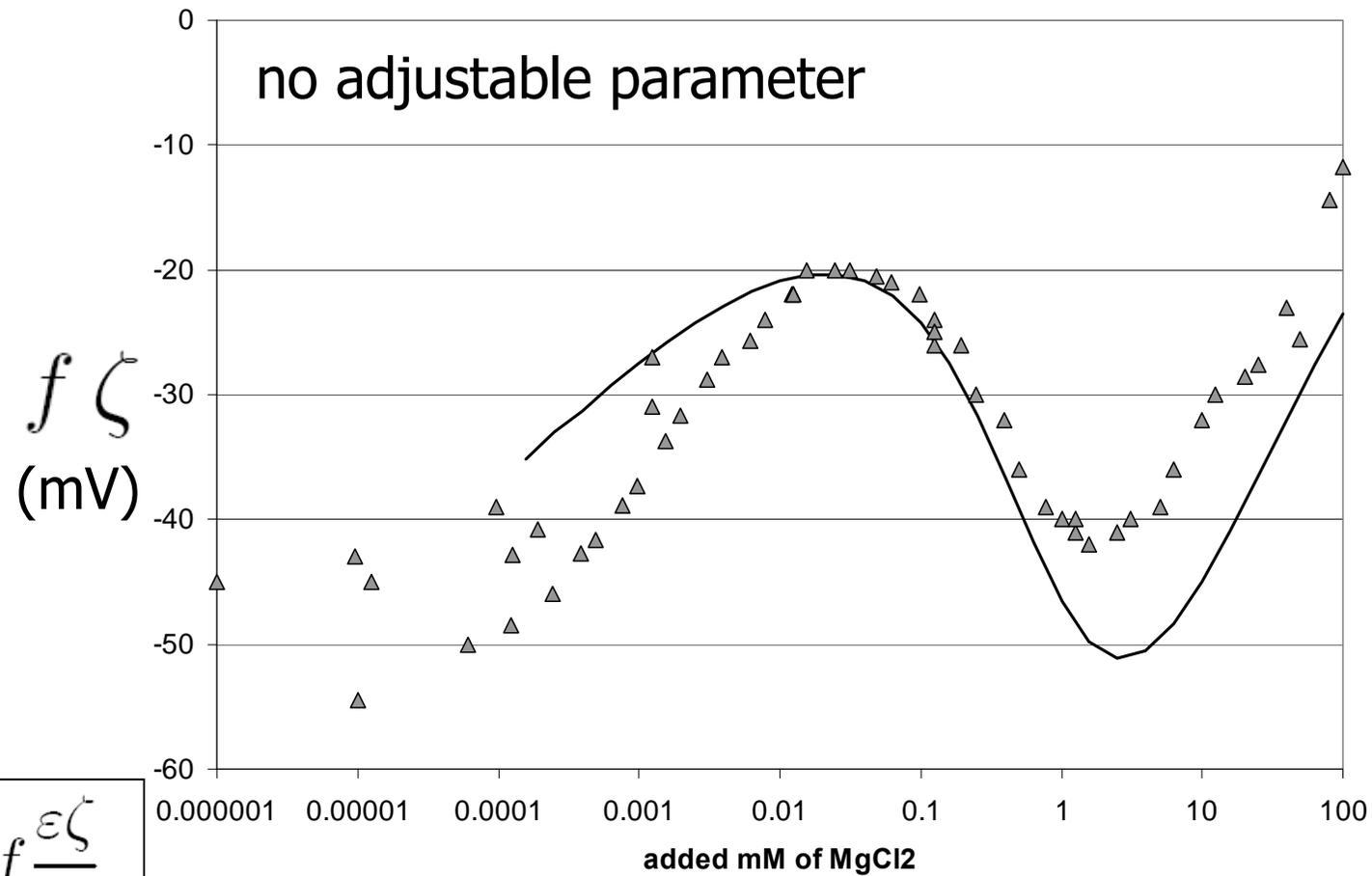
$$U = f \frac{\epsilon \zeta}{\eta}$$



X

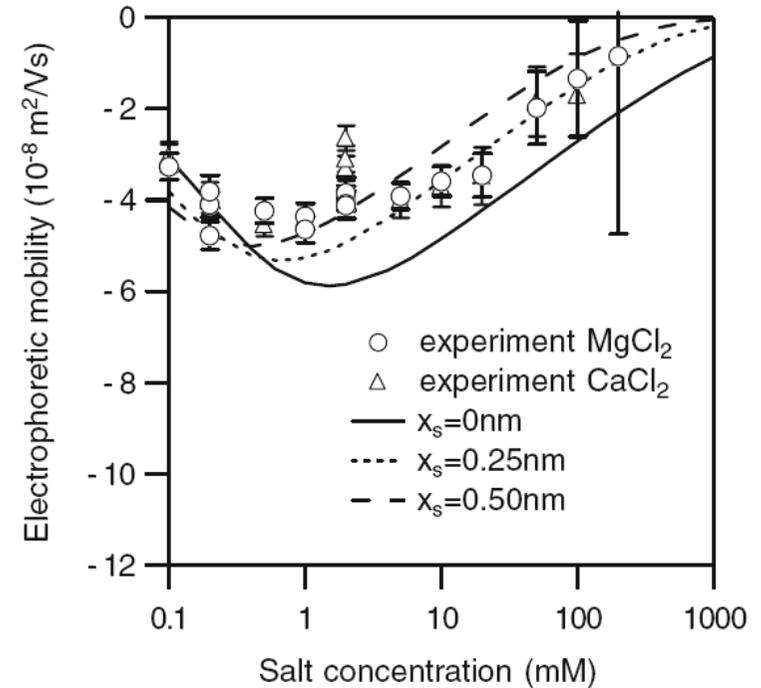
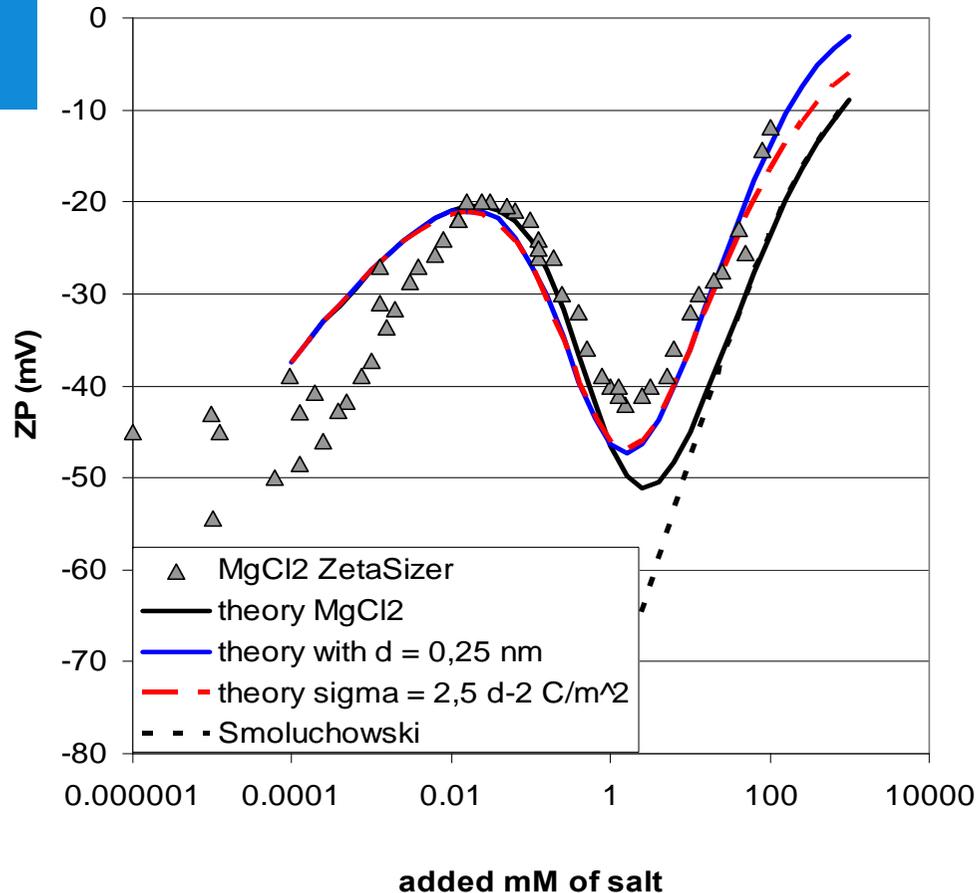


Electrophoresis / added salt constant charge



$$U = f \frac{\epsilon \zeta}{\eta}$$

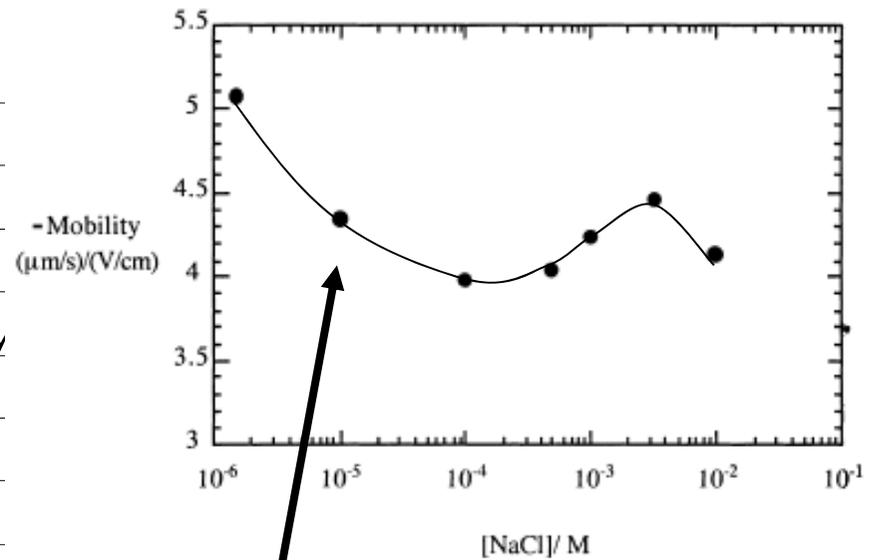
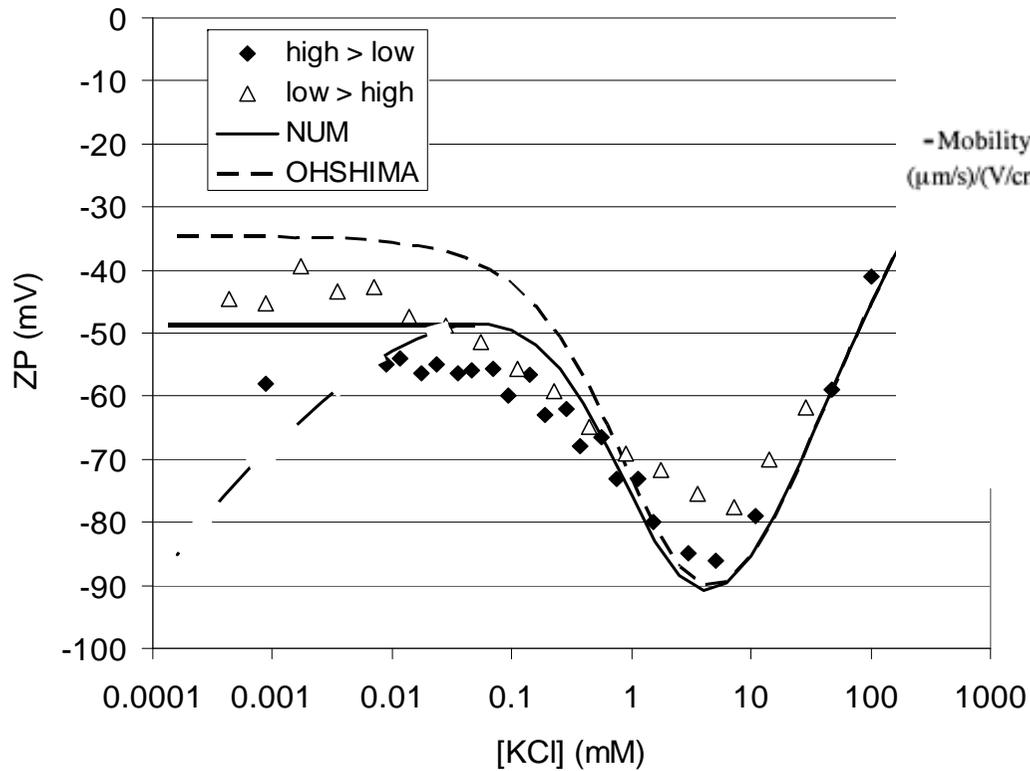
Electrophoresis / added salt constant charge



same behavior for 2800 nm
spheres (Kobayashi, Colloid
Polym Sci (2008) 286:935–940)

Electrophoresis / added salt constant charge

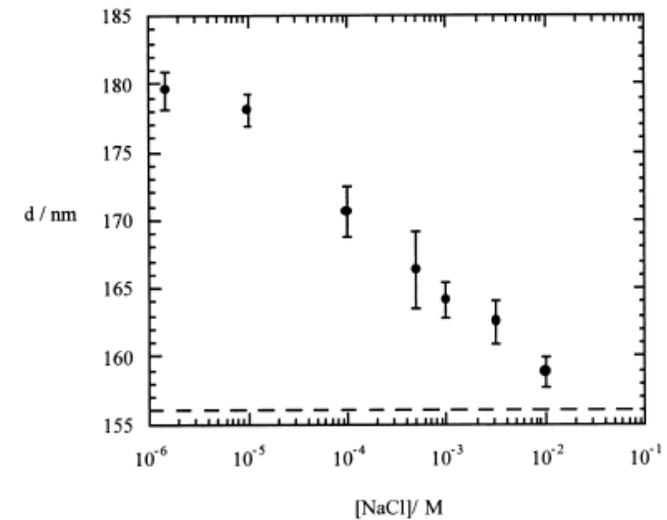
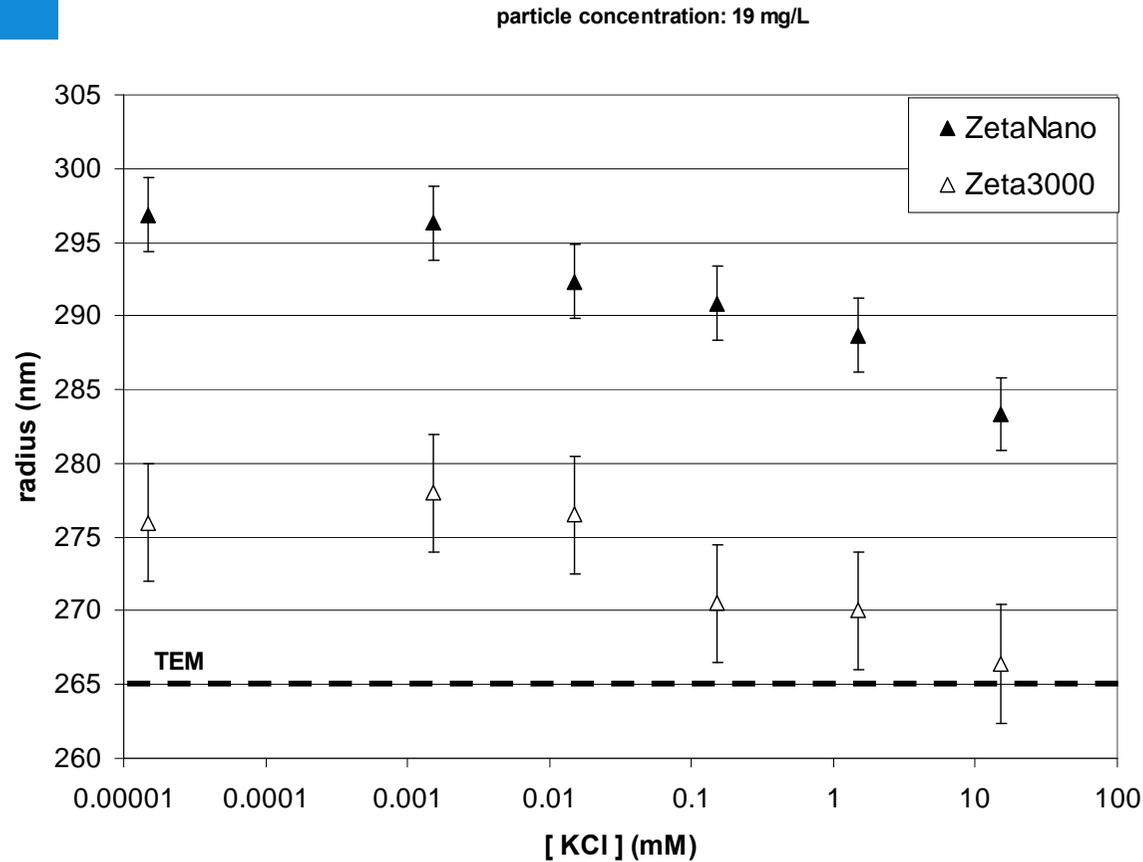
Gittings and Saville,
Colloids and Surfaces A
(1998)



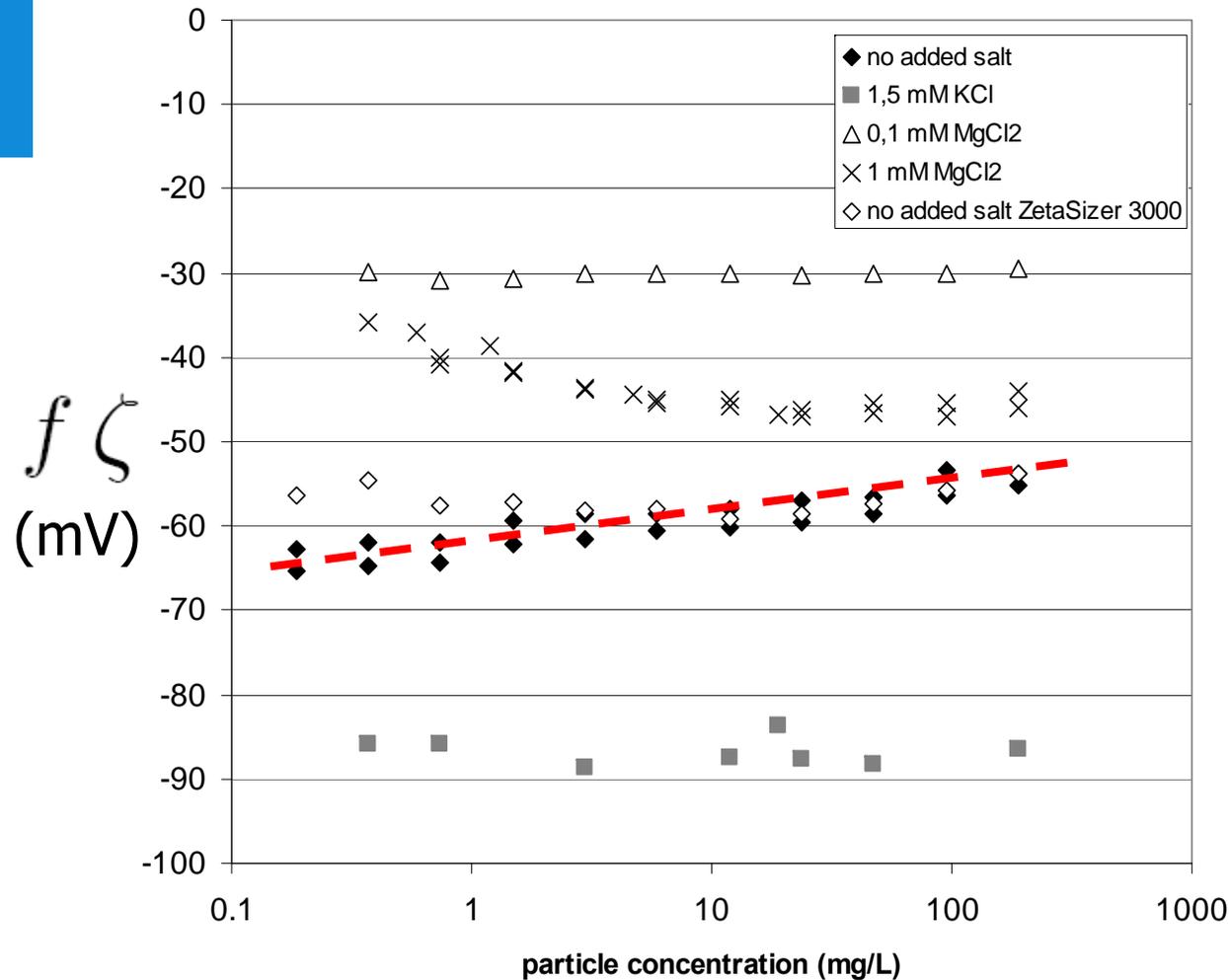
Hairy layer : Particle size / added salt

DLS and TEM

Gittings and Saville, Colloids and Surfaces A (1998)



Electrophoresis / particle concentration



"salt-free"
 $ZP \approx -\log(1/\Phi)$

Ohshima, Journal of Colloid and Interface Science
247, 18–23
(2002)

Summary for spheres

- Standard theory describes reasonably well the electrokinetic behavior of the latex particles, with no adjustable parameter (electrophoresis, dielec. spectro., conductivity)
- adding a Stern layer conductance does not improve the fit
=> hairy layer ("soft particles") could be explanation for shifting the shear plane approx. 0.25 nm from the particle surface
- behavior as function of particle volume fraction follows prediction for nearly no salt

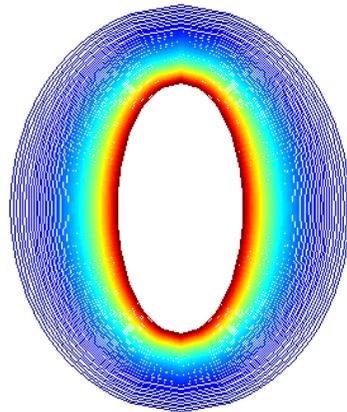
Outlook

electrokinetic response of spheroidal particles

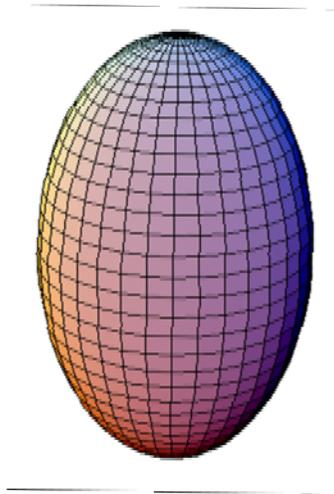
2008 : => analytical solution (reproduce O'Brien + Loewenberg)

C. Chassagne, D. Bedeaux / Journal of Colloid and Interface Science 326 (2008) 240–253

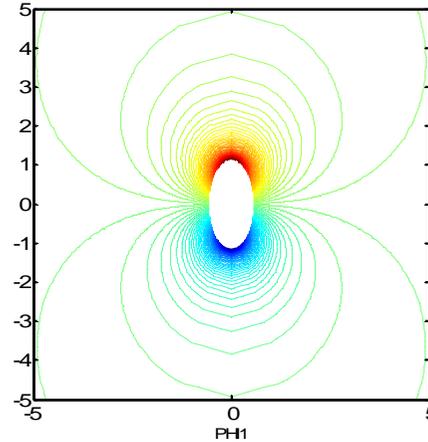
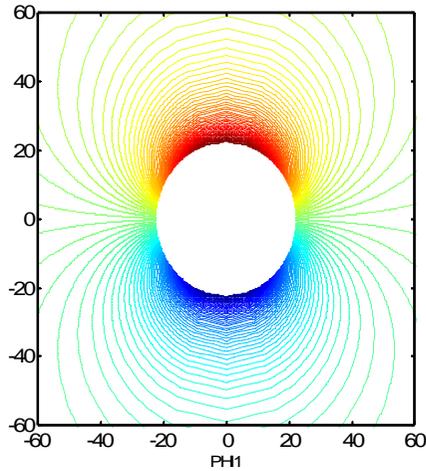
2012 : => numerical solution (=> improve analytical solution)



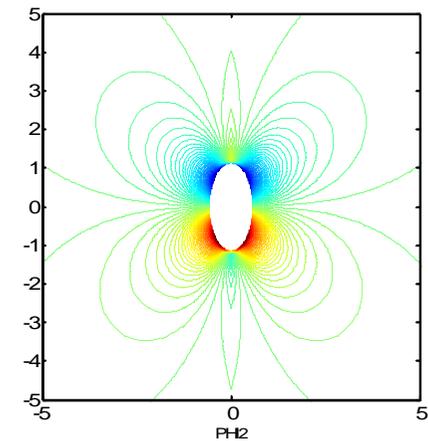
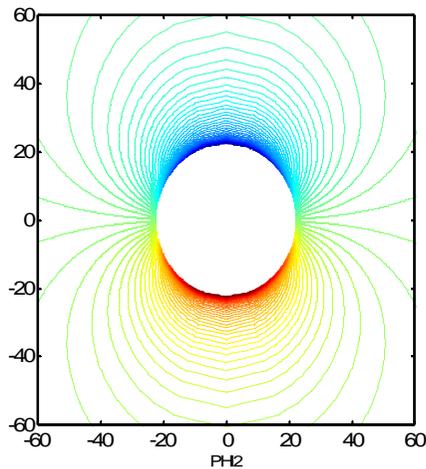
Prolate spheroids (cigars)



Prolate spheroids (cigars)

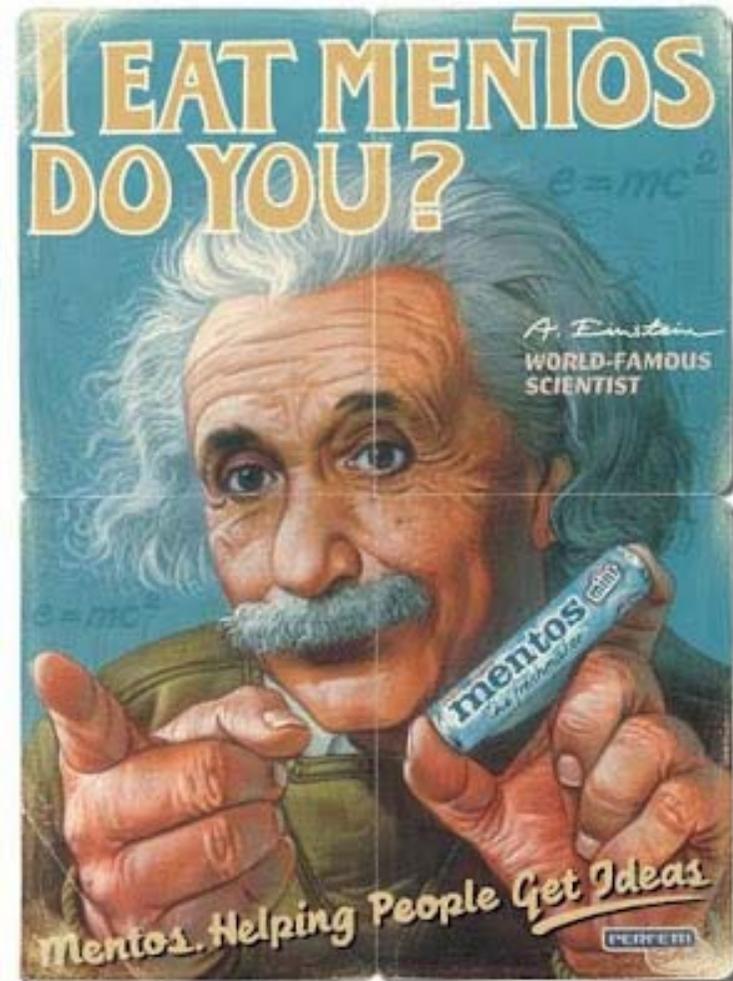
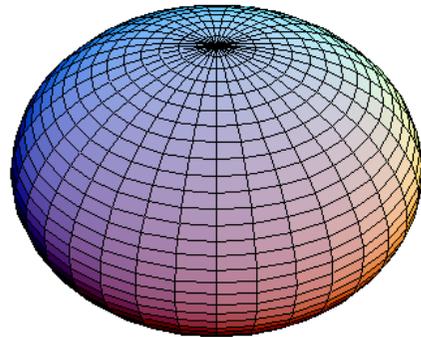


electrochemical
potential counterions



electrochemical
potential co-ions

Oblate spheroids (mentos)



Doppler electrophoresis at **low** volume fraction (original vol. frac. = 0.6%)

Gibbsite (original conc. : 16 mg/L)

