

# HOW TO CHARACTERIZE YIELD STRESS FLUIDS WITH CAPILLARY BREAKUP EXTENSIONAL RHEOMETRY (CABER)?

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## ABSTRACT:

Filament breakup of high viscosity fluids with apparent yield stress has been investigated and strategies for an appropriate characterization of their behavior in CaBER experiments are discussed. Filament profiles of such fluids exhibit significant concave curvature. Accurate determination of filament shape is mandatory for understanding deformation behavior. Therefore, we have set up an optical train including high-speed camera, telecentric objective and telecentric back-light illumination with a blue light emitting diode (LED) providing high contrast filament shape imaging. Image analysis allows for diameter determination with an accuracy of  $3.55 \mu\text{m}/\text{pixel}$ . In addition to the transient filament diameter at the neck we have extracted the curvature at this point as a function of time and the region of deformation, in order to characterize the extensional flow behavior. We have investigated the time evolution of filament shape as a function of various experimental parameters like stretching time, velocity profile during stretching, stretching ratio and initial sample volume at constant stretching ratio. Filament thinning is independent of stretching time,  $t_s$ , and stretching velocity profile. But when the same stretching ratio is applied at different initial volume fraction, filament curvature increases strongly with decreasing sample volume leading to an increase of filament life time according to the negative contribution of its curvature to the Laplace pressure inside the fluid.

## ZUSAMMENFASSUNG:

Es wurde der Fadenabriss von hochviskosen Flüssigkeiten mit scheinbarer Fließgrenze untersucht und Strategien für die Charakterisierung ihres Verhaltens in CaBER Experimenten diskutiert. Das Fadenprofil solcher Flüssigkeiten zeigt eine signifikante konkave Krümmung. Daher ist die präzise Charakterisierung der Fadenkonturen für das Verstehen des Deformationsverhaltens entscheidend. Aus diesem Grund wurde der optische Aufbau des CaBER Gerätes mit einer Hochgeschwindigkeitskamera, telezentrischen Objektiven und blauer, telezentrischer Hintergrundbeleuchtung, die eine kontrastreiche Fadenkonturabbildung ergibt, ausgestattet. Die Bildanalyse lässt eine hochauflösende Durchmesserbestimmung mit der Genauigkeit von  $\pm 3.55 \mu\text{m}/\text{pixel}$  zu. Zusätzlich zum zeitlichen Verlauf des Durchmessers an der Fadeneinschnürung wurden auch der zeitliche Verlauf der Krümmung an dieser Stelle und der Formänderungsbereich berechnet, um das Dehnfließverhalten zu charakterisieren. Die zeitliche Entwicklung der Fadenprofile in Abhängigkeit von unterschiedlichen experimentellen Parametern wie z. B. Dehnzeit  $t_s$ , Dehngeschwindigkeitsprofil, Dehnrate und Anfangsprobenvolumen bei konstanter Dehnrate wurde untersucht. Die Fadenverdünnung ist unabhängig von  $t_s$  und dem Dehngeschwindigkeitsprofil. Wird die gleiche Dehnrate bei unterschiedlichem Anfangsprobenvolumen verwendet, steigt die Fadenkrümmung mit abnehmendem Probenvolumen stark an. Dies führt zur Erhöhung der Fadenlebensdauer entsprechend dem negativen Beitrag der Krümmung zum Laplace Druck innerhalb der Flüssigkeit.

## RÉSUMÉ:

La rhéologie extensionnelle de fluides de viscosité élevée ayant une contrainte seuil a été étudiée dans le but d'obtenir des connaissances déterminantes sur leur comportement lors de ce type d'écoulement. Les expériences ont été effectuées à l'aide du rhéomètre élongationnel CaBER. Le profil des filaments obtenu pour de tels fluides montrent une courbure concave significative et une détermination précise de leurs formes est nécessaire pour comprendre leur comportement lors de la déformation. Pour cela nous avons équipé notre montage optique d'une caméra à haute vitesse, d'un objectif télécentrique et d'un éclairage d'arrière-plan télécentrique de couleur bleue qui permet d'obtenir un contraste élevé de l'image du filament. L'analyse des images au point de courbure du filament permet une détermination du diamètre au cours du temps avec une précision de l'ordre de  $3.55 \mu\text{m}/\text{pixel}$ . En plus de la détermination du diamètre, nous avons également étudié l'évolution de la forme de la courbure du filament en fonction du temps en variant divers paramètres expérimentaux tels que : la durée de l'élongation, le profile de vitesse durant l'élongation, le taux d'élongation et le volume initiale de

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ware. The time evolution of the full filament contour is detected with resolution of  $\pm 1$  pixel.

The influence of the stretching parameters of the CaBER device on capillary thinning of fluids with an apparent yield stress was discussed. Neither stretching time nor stretching velocity profile has significant influence on the capillary thinning of those fluids. Suggested initial set-up parameters are cushioned stretching profile, which provides the best reproducible results and optimal stretching time is in the range between 35 ms and 50 ms. Variation of Hencky strain, results in a decrease of initial diameter and filament life time with increasing  $\epsilon$ , but it has no influence on the initial curvature. Moreover, diameter and curvature at the neck, measured for different  $\epsilon$  show similar time evolution. Lastly, if plate separation is varied in a way that keeps Hencky strain unchanged, the initial value of diameter remains constant but the curvature increases with decreasing initial gap separation and results in a deceleration of the thinning process according to the corresponding drop of the Laplace pressure inside the filament.

Although further efforts are required for a determination of physical quantities like elongational viscosity, the CaBER technique can be successfully applied to investigate elongational flow properties of yield stress fluids. The time- and space- evolution of the fluid filament can be quantified. The measurement technique gives well reproducible results, variation in the characteristic parameters extracted from the filament profiles do not exceed 10 %. Thus, future work will address influence of fluid properties, e.g. volume fraction of disperse phase and droplet size for the emulsions or polymer concentration and pH value for the thickener solutions, on capillary thinning. The determination of an elongational yield stress and the identification of rheological parameters characterizing the transient extensional properties of such fluids which can be correlated to processing and application properties will be of particular interest.

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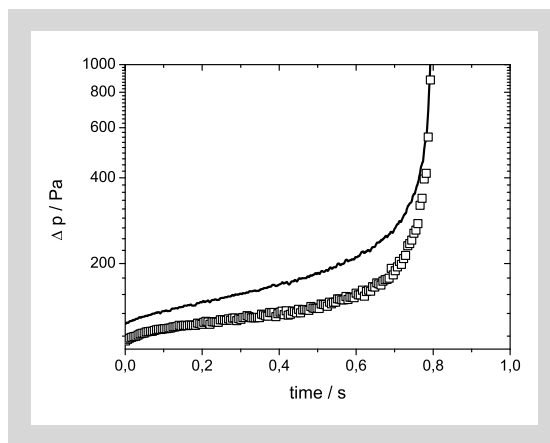


Figure 12: Influence of filament curvature on Laplace pressure. The open symbols show the Laplace pressure calculated from Eq. 4 using the data from Figure 11 (a) and (b). The initial plate distance was  $h_0 = 1.5$  mm, and end plate distance,  $h_f = 16.64$  mm. Solid line was calculated neglecting the filament curvature, i.e.  $R_2 = 0$ .

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